

Object A of mass 5 kg slides along a frictionless surface at a speed of 3 m/s. It is hit by object B moving at a speed of 6 m/s from behind. The two objects stick together and move at a speed of 4 m/s. What is the mass of object B.

Given:

Mass of A:

$$m_A = 5 \text{ kg}$$

Initial speed of A:

$$v_{iA} = 3 \text{ m/s}$$

Initial speed of B:

$$v_{iB} = 6 \text{ m/s}$$

Final speed of the A+B

$$v_f = 4 \text{ m/s}$$

Determine: Mass of B: m_B

Use the law of conservation of momentum: For an isolated system, the total initial momentum, p_i , of the system is equal to the total final momentum, p_f , of the system.

$$p_i = m_A v_{iA} + m_B v_{iB} \dots \dots \dots (1)$$

$$p_f = (m_A + m_B) v_f \dots \dots \dots (2)$$

Since $p_i = p_f$:

$$m_A v_{iA} + m_B v_{iB} = (m_A + m_B) v_f \dots \dots \dots (3)$$

Substituting for m_A , v_{iA} , v_{iB} , and v_f in (3):

$$(5 \times 3) + (m_B \times 6) = (5 + m_B) \times 4 \dots \dots \dots (4)$$

Rearranging (4):

$$m_B = 5 / 2 = 2.5 \text{ kg}$$